Palace Wood Primary School Progression in Calculations Policy



Palace Wood Primary School

Written by	Emily Carpenter	
Date for Review	Spring 2021	
Signed – Headteacher		

This policy has been impact assessed by Emily Carpenter in order to ensure that it does not have an adverse effect on race, gender or disability equality

Palace Wood Primary School – Calculation Progression

This policy is based on national expectations as outlined in the 2014 National curriculum. Year groups are included but teachers will need to use a degree of flexibility in deciding appropriate methods for different groups of children.

Updated by Emily Carpenter 2018

To be used in conjunction with all other progression documents linking to the programmes of study, notably fractions, reasoning and algebra.

Introduction:

The 2014 National Curriculum provides a structured and systematic approach to the teaching of calculation. The aim is for mental calculations and written procedures to be performed efficiently, fluently, accurately with understanding. Procedures and understanding are to be developed in tandem. End of key stage expectations are explicit in the programme of study.

At Palace Wood Primary School, we have a consistent approach to the teaching of written calculation methods in order to ensure continuity and progression across the school.

Age related expectations:

This calculation policy is organised according to age appropriate expectations as set out in the National Curriculum 2014, however it is vital that pupils are taught according to the stage that they are currently working at, being moved onto the next level as soon as they are ready, or working at a lower stage until they are secure enough to move on.

Providing a context for calculation:

It is important that any type of calculation is given a real life context or problem solving approach to help build children's understanding of the purpose of calculation, and to help them recognise when to use certain operations and methods. It is also important for children to be confident to use mental and/or written strategies to explain their thinking. This must be a priority within calculation lessons. Written methods need to be viewed as tools to enable children to solve problems and record their thinking in an organised way.

Aims:

Children should be able to use an efficient method, mental or written appropriate to the given task, with understanding. Children are encouraged to use a range of models and images, such as arrays, the bar method, number lines to ensure they understand the final compact method they are building up to. By the end of year 6, children will have been taught, and be secure with, a compact standard method for each operation.

To develop efficient written calculation strategies children need:

- Secure mental methods which are developed from early years
- A solid understanding of the number system and place value
- Practical hands on experience including a range of manipulatives spanning all of the vear groups
- Visual models and images including number lines and arrays
- Experience of expanded methods to develop understanding and avoid rote learning

- The ability to explain each step of the calculation and explain WHY each step is done using appropriate vocabulary
- Secure understanding of each stage before moving onto the next.

Before carrying out a calculation, children will be encouraged to consider:

- Can I do it in my head? (using rounding, adjustment)
- The size of an approximate answer (estimation)
- Could I use jottings to keep track of the calculation?
- What is the most appropriate way to answer this calculation?
- Which resources to use to support their calculation.

When are children ready for written calculations?

Addition and subtraction:

- Do they know addition and subtraction facts to 20?
- Do they understand place value and can they partition numbers?
- Can they add three single digit numbers mentally?
- Can they add and subtract any pair of two digit numbers mentally?
- Can they explain their mental strategies orally and record them using informal jottings?
- Are the children able to explain the process of addition and substraction?

Multiplication and Division:

- Do they know the 2, 3,4,5,6 and 10 times tables and corresponding division facts?
- Do they know the result of multiplying by 1 and 0?
- Do they understand 0 as a place holder?
- Can they multiply two and three digit numbers by 10 and 100?
- Can they double and halve two digit numbers mentally?
- Do they understand the relationship between multiplication and division?
- Can they use multiplication and division facts they know to derive mentally other multiplication and division facts that they do not know?
- Can they explain their mental strategies orally and record them using informal jottings?

These lists are not exhaustive but are a guide for the teacher as they structure the move from informal to formal methods of calculation. It is important that children's mental methods of calculation are practised, taught and secured alongside their learning and use of an efficient written method for each operation. Additionally, key number skills should be continually revisited to ensure that every child's understanding of concepts in number supports his/her development in calculation and these areas should be taught explicitly/revisited if the need arises either in whole class lessons or in guided groups.

A pathway to teaching calculation methods:

Expanded methods should be viewed as steps towards a standard method and not as methods in themselves.

Before beginning to record in a more refined written format, children must have had significant practical work reinforced with appropriate manipulative, models and images.

Teachers will guide pupils to refine their written methods of recording by modelling and asking questions such as "What is the same? What's different? What mistakes can you spot?"

Learning will be planned to ensure pupils are encouraged to use and apply what they have learnt to problem solving tasks and a range of contexts.

As children move along the pathway, it is vital that they practice, reinforce, consolidate, use and apply it to mathematical learning and NOT simply move onto the next step.

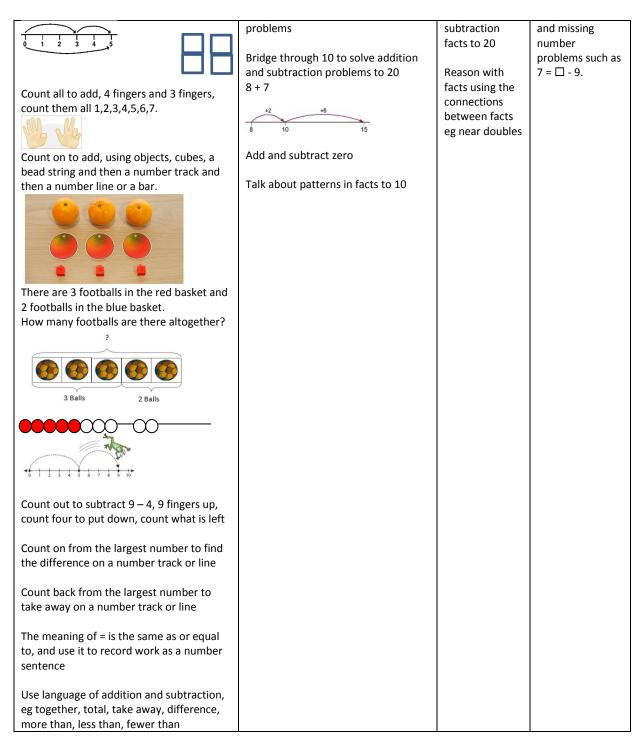
Points to note:

- To be successful in learning to calculate children must be able to; count reliably forwards and backwards, recognise individual digits, know what each digit represents, know that digits combine to make numbers and have some understanding of the concept of zero.
- The correct terminology should be used by <u>all</u> staff <u>and</u> children when referring to the value of digits to support the children's understanding of place value. e.g. 68 + 47 should be read 'sixty add forty' not 'six add four'
- Teachers should refer to the programme of study for key vocabulary for each year group.

Palace Wood Primary school has a Maths Specialist Teacher hence we are following Canterbury Christ Church's progression in calculations. Our thanks go to CCCU for allowing us to use and edit the following document.

Year 1 Addition and subtraction

Term 1 and 2	Term 3 and 4	Term 5 and 6	End of year
Combining two groups to solve addition	As before and	As before and	read, write and
problems			interpret
	Count forwards and backwards along	Rapid, fluent	mathematical
	a number line from any number and	recall of	statements
	relate to addition and subtraction.	addition facts	involving
		to 10	addition (+),
Increasing one group to solve addition	Commutative law for addition, but		subtraction (-)
problems	not for subtraction, using concrete	Use number	and equals (=)
problems	objects such as Cuisenaire rods and a	facts to 20 to	signs
	number line to 'prove' this.	solve one step	
		problems and	represent and
Partitioning one group in to two to solve	Count on from the largest number to	record with a	use number
subtraction problems	add, and know that I can count on	number	bonds and
4	from either number	sentence and	related
		with practical	subtraction facts
	Make connections between addition	resources and	within 20
	and subtraction to 10, moving	images such as	
	forwards and backward along a	number lines	add and subtract
Take away from one group and use it to	number line, and then using one		one-digit and
solve subtraction problems	number fact to list others	Reorder	two-digit
		numbers to add	numbers to 20,
	Make connections between number	them more	including zero
	facts eg use 4 + 4 = 8 to calculate 4 +	easily using	
	5	known number	solve one-step
Use addition or subtraction to solve		bonds to 10 eg	problems that
problems about difference:	Solve missing number problems, with	3 + 8 + 7	involve addition
What is the difference between 2 and 5? If	the unknown in different places. Use		and subtraction,
I have 3 stickers how many more do I need	the bar method.	Make	using concrete
to have 5?		connections	objects and
	Use addition and subtraction facts to	between	pictorial
	10 to work out facts to 20 to solve	addition and	representations,



Year 2 Addition and subtraction

Term 1 and 2	Term 3 and 4	Term 5 and 6	End of year
Begin to recall number facts to 20,	As before and	As before and	solve problems with
including addition and subtraction			addition and
facts, use patterns and connections	Missing number problems	Rapid , fluent recall of	subtraction:
between addition and subtraction	up to 20	number facts to 20	using concrete
			objects and pictorial
Know all doubles of numbers up to	Make connections between	Make connections between	representations,
20	number facts to 10 and 20,	number facts to 10 and 20,	including those
	and number facts to 100,	and number facts to 100	involving numbers,
Solve problems including:	working with multiples of	7 + 3 = 10	quantities and

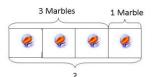
- -Combining two groups
- -Adding to one group
- -Partitioning one group
- -Taking away
- -Comparing two amounts to state the difference, how many more or less, and how many to make them equal
- -Experience subtraction as difference and take way, counting back from the first number, or up from the smallest number on a number line

Add and subtract numbers using concrete objects, pictorial representations and symbols, related to real life problems and measures. including:

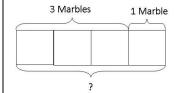
- -add three one digit numbers (looking for facts to help such as reordering to match numbers which total 10)
- add and subtract any unit number to a multiple of ten on a number line or with Dienes

Show that addition of two numbers can be done in any order (commutative) and subtraction of one number from another cannot, using resources or a number line or the bar method

Peter has 3 marbles. Harry gives Peter 1 more marble. How many marbles does Peter have now?



Progress from concrete to abstract.



ten
7 + 3 = 10
70 + 30 = 100

Know all doubles of multiples of ten to 100

To state what must be added to a number to take it to the next multiple of 10 52 +? = 60

Given one number fact to 100, list all related number facts

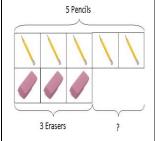
Use and understand language of addition and subtraction, including sum and difference

Add and subtract numbers using concrete objects, pictorial representations and symbols, related to real life problems and measures. including:

-add and subtract any two digit number and a units number for example on a number line or empty number line, including bridging through a multiple of ten



- -add and subtract any two digit number and a tens number on a number line or with Dienes
- use the bar comparatively Peter has 5 pencils and 3 erasers. How many more pencils than erasers does he have?

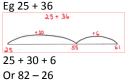


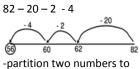
23 + 67 = 100 Using Dienes apparatus, a number line or the empty number line for example

Solve problems and puzzles with numbers up to 100, including those with numbers, quantities and measures using concrete resources or images such as an empty number line or the bar method

Check answers using the inverse operation, or by adding in a different order

Add and subtract any two digit numbers -partition one number and keep one number whole





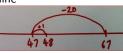
prepare for column addition; (addition only) 25 + 30

20 + 30 = 50 5 + 6 = 11

5 + 6 = 1150 + 11 = 61

Use dienes or place value counters

-add or subtract 9, 19, 29, 11, 21 etc by adding and subtracting multiples of ten and adjusting on a number line



67 – 19= 67 – 20 + 1 -Use near doubles Use 25 = 25 = 50 to calculate 25 + 26

measures applying their increasing knowledge of mental and written methods

recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100

add and subtract numbers using concrete objects, pictorial representations , and mentally, including: a two-digit number and ones; a twodigit number and tens; two two-digit numbers; adding three one-digit numbers

show that addition of two numbers can be done in any order (commutative) and subtraction of one number from another cannot

recognise and use the inverse relationship between addition and subtraction and use this to check calculations and missing number problems.

Year 3 Addition and subtraction

Term 1 and 2	Term 3 and 4	Term 5 and 6	End of year
Recall of number facts to	As before and	As before and	,
100, including doubles and			add and subtract
halves of numbers up to 100	Estimate the answer to a calculation and use	Fluent mental	numbers
	inverse operations to check solutions.	addition and	mentally,
Count on and back in units,	·	subtraction with	including:
tens and hundreds	Fluent mental addition and subtraction with	numbers above 100	-a three-digit
	numbers up to 100		number and
State what needs to be		Column methods	ones
added to a number to make	Column methods with addition and subtraction	with addition and	-a three-digit
the next multiple of 100	for two digit numbers, starting with an	subtraction for	number and tens
	expanded form and moving to the formal	three digit	-a three-digit
Use of mental strategies	method. Use of Dienes or place value counters	numbers, starting	number and
covered in Year 2 for facts to	for example alongside written methods. Link	with an expanded	hundreds
100 not remembered, such	with place value and exchanging ten units for a	form and moving to	
as:	ten. (Swap a block game.)	the formal method.	add and subtract
-reordering numbers when	Addition:	Use of Dienes or	numbers with up
adding to match pairs of		place value	to three digits,
numbers for example which total multiples of 10 or 100,		counters for	using formal written methods
Eg 24 + 37 + 36 = 60 + 37	0.5	example alongside written methods.	of columnar
-partitioning one number	25 +47	Link with place	addition and
and keeping one number		value and	subtraction
whole, Eg 58 - 21		exchanging ten tens	Subtraction
	0000	for a hundred.	estimate the
37 47 57 58	000	(Swap a block	answer to a
\circ	25	game.)	calculation and
-partitioning both numbers	+47.©		use inverse
for addition only,		8 12 1	operations to
-bridging through multiples		9 3 2	check answers
of ten, eg 82 - 26	• •	- 4 5 7	
2			solve problems,
\$6 60 80 82	25	4 7 5	including missing
-adding or subtracting a	+47		number
larger or small number and	72		problems, using
then adjusting			number facts,
Eg 82 - 26	Subtraction:		place value, and
+4	Tens Ones		more complex
52 68 82			addition and subtraction.
	• • • · · · · · · · · · · · · · · · · ·		Subtraction.
Add and subtract, using a	-47		
number line or Dienes			
apparatus for example at			
first, and then	Tens Ones		
mentally including;			
-a three digit number and a	○ ○ ○ 次2		
unit number	-47		
- a three digit number and a			
multiple of ten			
-a three digit number and a			
multiple of one hundred	Tens Ones		
Calva muchlanes in shorting			
Solve problems, including	** ° ° ° ° ° ° ** 2 ** 47		
missing number problems, using number facts, place			
value, and more complex			
addition and subtraction.			
addition and subtraction.			
	Could move onto the expanded method for		

addition/subtraction to ensure that children are able to fully understand and explain the value of the digits within the calculations 245 + 352 50 13 7 300 60 3 90 - 100 20 7 500 200 30 6 597	
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Year 4 Addition and subtraction

Term 1 and 2	Term 3 and 4	Term 5 and 6	End of year
Rapid and fluent recall and use of	As before and	As before and	add and subtract
facts up to and beyond 100.			numbers with up
		Rapid and fluent	to 4 digits using
Strategies to work out facts which	Addition of numbers up to	recall of number	the formal
cannot be remembered such as;	4 digits using formal,	facts involving	written methods
-reordering numbers when adding,	column addition, drawing	tenths	of columnar
- keeping one number whole and	on place value knowledge		addition and
partitioning the other number,	that ten hundreds is one	Subtraction of	subtraction
counting forwards or backwards in	thousand, showing this	numbers with up to	where
ones, tens or hundreds perhaps with	with Dienes and place value	4 digits using	appropriate
dienes or on an empty number line	counters.	formal, column	
Eg 132 - 28		subtraction, drawing	estimate and use
20	7 8 9	on place value	inverse operations to
103 111 132	+ 6 4 2	knowledge that one	check answers to a
132		thousand is ten	calculation
eg 236 – 172 = 236 – 100 – 70 - 2	1 4 3 1	hundreds, showing	carcaration
-partitioning both numbers for	1 1	this with Dienes and	
addition only,		place value	solve addition and
-bridging through multiples of ten on		counters.	subtraction two-step
an empty number line,			problems in contexts, deciding which operations
-adding or subtracting a larger or		Solve addition and	and methods to use and
small number and then adjusting		subtraction two-	why.
Eg 367 – 198 = 367 – 200 + 2		step problems in	willy.
near doubles and halves eg 180 -		contexts, deciding	
91		which operations and methods to use	
-subtract by finding the difference by		and methods to use	
counting up from the smaller		and why.	
number, especially when the		4070.00	
numbers are close together or by		1073.00	
taking away from the larger number		+ 54.20 7.09	
on an empty number line		1134.29	
		1134.23	
Estimate the answers to addition			
and subtraction problems, and use			
inverse operations to check solutions			
inverse operations to check solutions			
Solve addition and subtraction one			
step problems in contexts, deciding			
which operations and methods to			
use and why.			
,			

Year 5 Addition and subtraction

rm 1 and 2	Term 3 and 4	Term 5 and 6	End of year
ord recall and fluent use of dition and subtraction facts, luding those with decimal mbers and with numbers ove 1000 e of mental strategies to work tracts which cannot be membered such as: ordering numbers when ding, 1.2 + 0.43 + 0.8 = 2 + 0.43 eeping one number, unting forwards or backwards nundredths, tenths, ones, tens hundreds perhaps with dienes on an empty number line 2358 - 1136 = 2358 - 1000 - 0 - 30 - 6 irritioning both numbers for dition only, 3.4 + 5.2 5 - + 0.2 idging through multiples of a on an empty number line, lding or subtracting a larger or all number and then adjusting 4.3 + 2.99 = 4.3 + 3 - 0.01 itear doubles and halves, and own number facts eg using 68 at to calculate 680 + 430, 6.8 + 4, 0.68 + 0.43 btract by finding the ference by counting up from a smaller number, especially en the numbers are close gether or by taking away from elarger number on an empty mber line	As before and Add and subtract whole numbers with more than 4 digits including decimals, using formal written methods in columns, using drawing on place value knowledge and showing this with Dienes and place value counters.	Term 5 and 6 As before and Use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy Solve increasingly complex addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why.	End of year add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction) add and subtract numbers mentally with increasingly large numbers use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why.

Year 6 Addition and subtraction

Term 1 and 2	Term 3 and 4	Term 5 and 6	End of year
Perform mental calculations, including with mixed operations and large numbers, and those with digits after the decimal point using rapid recall and fluent use of strategies such as: -count on and back in steps of thousands, or hundreds, tens, tenths hundredths, thousandths etc -use knowledge of place value to calculate new facts from those already known	Term 3 and 4 As before and Explore the use of brackets for eg 2 + 1 x 3 and (2 + 1) x 3 and precedence rules such as BODMAS and state as a general rule Use of formal written methods for addition and subtraction with any size number Round answers to a given degree of accuracy eg to the	Term 5 and 6 As before and Explore addition and subtraction within algebra eg think of a number problem Think of a number (no bigger than 20) Add 5 Double the answer Subtract 4 Halve the answer Take away the number you first thought of Why is your answer always 3?	perform mental calculations, including with mixed operations and large numbers use their knowledge of the order of operations to carry out calculations involving the four operations solve addition and subtraction multi-step problems in contexts, deciding which operations
	_		and methods to use and why solve problems involving addition, subtraction, multiplication and division use estimation to check answers to calculations and determine, in the context of a problem, an appropriate
subtraction multi-step problems in contexts, deciding which operations and methods to use and why Use brackets in simple number sentences			degree of accuracy.
Solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why Use estimation to check answers to calculations and			

determine, in the context of a problem, an appropriate degree of accuracy.		

Year 1 Multiplication and Division

Term 1 and 2	Term 3 and 4	Term 5 and 6	End of year
Explore multiplication as repeated addition using	As before and	As before and	Solve one-step problems involving multiplication and
resources and real life	Explore multiplication as an	Explore multiplication as	division, calculating the
contexts	array, showing items in	scaling eg using cubes to	answer by using concrete
Contexts	rows or columns of 2, or 5	make a tower and then	objects, pictorial
Talk about one to many	or 10.	make it twice as high	representations and arrays
relationships, eg one car, 4		and the state of t	with the support of the
wheels, one pair of gloves,	Half amounts practically	Count in 2s, 5s and 10s,	teacher.
two gloves etc	, ,	forwards and backwards.	
	Record halves and doubles	Recognise and use the	
Count in ones forwards and	informally	patterns in the digits units in	
backwards		the multiples of 2, 5 and 10.	
	Count in tens and twos		
Rhythmic counting in ones,		Make connections between	
eg shout and whisper		multiplication and division	
alternate numbers		eg repeated addition and	
		repeated subtraction or	
Double amounts practically		grouping	
		Draw pictures to show equal	
Explore division using		sets.	
resources and real life		3 sets of 3 make 9	
contexts as:		XXX XXX XXX	
 sharing with a focus on equal shares eg share 		2 sets of 4 make 8	
12 stickers between		XXXX XXXX	
three children		AAAA AAAA	
grouping or repeated		Draw pictures to show	
subtraction with a		sharing and grouping. Show	
focus on equal groups		inverse.	
eg how many cars can		9 shared between 3	
you put wheels on if		XXX XXX XXX	
you start with 16			
wheels?		How many groups of 4 in 8?	
		хххх хххх	
Solving real problems, often			
in play and recording		Solve one step problems	
informally		involving multiplication and	
		division	
		Find simple fractions of	
		objects, numbers and	
		quantities and link to	
		division eg ½ or 1/4	
		Identify odd and even	
		numbers to 20	

	Make connections between	
	arrays, patterns and	
	counting in 2s, 5s and 10s.	
	Rapid recall of doubles to	
	10 and corresponding	
	halves	

Year 2 Multiplication and Division

real 2 Multiplication and Division			
Term 1 and 2	Term 3 and 4	Term 5 and 6	End of year
Explore 2x, 5x and 10x facts as repeated addition, and as an array, and as scaling, eg making a group or tower 2x, 5x or 10 larger Record multiplication and division facts for 2x, 5x and 10x using pictures and resources Solve problems eg find the total of	As before and Begin to recall and use 2x, 5x and 10x facts Begin to use symbols to record number facts	As before and Rapid recall of and fluent use of 2x, 5x and 10x facts Record multiplication and division facts for 2x, 5x and 10x using symbols x 2 = 20	recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers calculate mathematical statements for multiplication and division within the
numbers of objects when they are organised in groups of 2, 5 or 10, or divide objects into groups of 2, 5 or 10 or make groups of 2, 5 or 10 to solve division problems. Use a variety of language for multiplication eg groups of, twice as many, times, multiplied by, rows and columns Link multiplication and division facts for 2x, 5x and 10x 7 x 5 = 35 5 x 7 = 35 35 ÷ 5 = 7 35 ÷ 7 = 5 Solve multiplication and division problems using resources and arrays practically or draw on squared paper. Use a variety of language for division, number of groups of, shared between 3 lots of 2 2 lots of 3 'groups of' 3 x 2 = 6 Make connections between multiplication and division, showing this practically with resources, on a number line or with an array	Link 5x to the clock face Make connections between 10x and place value using Dienes Show that division is not commutative eg 10 divided by 2 is not the same as 2 divided by 10 Identify odd and even numbers to 100 Multiply and divide by 2, 5 and 10 with continuous quantities such as pieces of string, or water Link division to finding a fraction of an amount or quantity eg 3/4 Rapid recall and fluent use of doubles up to 20 and corresponding halves, rapid recall and fluent use of doubles of multiples of 10 to 50, and corresponding halves	Solve problems involving multiplication and division, using materials, arrays, repeated addition and subtraction, mental methods, and multiplication and division facts, including problems in contexts. Begin to explore multiplication by other numbers such as 3, 4 and 8 as repeated addition, as an array and as scaling, and division by other numbers such as 3, 4 and 8 as sharing and grouping. Find doubles of numbers up to 100 and corresponding halves by partitioning and doubling tens and units and recombining	multiplication tables and write them using the multiplication (×), division (÷) and equals (=) signs show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts.
Explore the commutative law for 2x 5x and 10x eg 2 x 5 = 5 x 2,			

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showing this with repeated addition, on a number line and as		
an array		

Year 3 Multiplication and Division

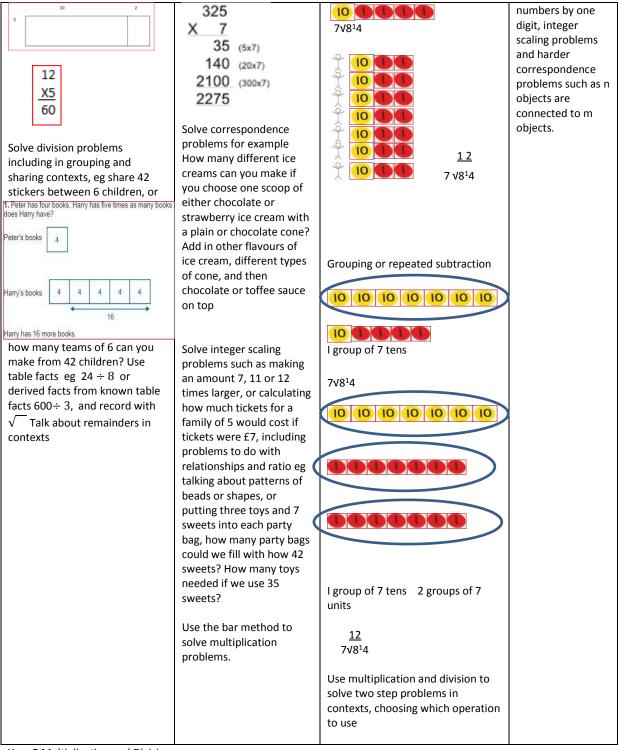
number itself.

Term 1 and 2 Term 3 and 4 Term 5 and 6 End of year Explore 3x table as repeated addition, As before and As before and recall and use arrays and scaling, eg making a tower multiplication and division 3 times as tall or an amount 3 times Explore 4x table as repeated Explore 8x table as repeated facts for the 3, as many addition, arrays and scaling, eg addition, arrays and scaling, e.g. 3x3= making a tower 4 times as tall eg making a tower 8 times as 4 and 8 tall or an amount 8 times as XXX XXX XXX or an amount 4 times as many multiplication tables manv Look for patterns in the 4x Multiply whole numbers by 0, 1, table, make links between 2 x Look for patterns in the 8x write and 10,100 4, 4 x 4, 8 x 4 etc table, make links between 2 calculate Make connections between x 8, 4 x 8, 8 x 8 etc mathematical Look for patterns in the multiples of multiplying by 2 and 4 by Make connections between statements for 3, make links between 2 x 3, 4 x 3, 8 x doubling multiplying by 2, 4 and 8 by multiplication doubling and division Practice recall of 4 x table using the Practice recall of 3x table Practice recall of 8x table multiplication Make links between tables that Make links between multiplying and multiplying and dividing by 4 Make links between they know, multiplying and dividing by 8, dividing by 3, showing this practically showing this practically or with including for or with an array or on a number line an array or on a number line showing this practically or two-digit e.g. 5 x 4 with an array or on a number numbers times Rapid recall and fluent use of one-digit 4s table numbers, using mental and Explore multiplying TU Rapid recall and fluent use of Ans=20 progressing to numbers by 2,5, 10, 3 and 4. 3,4x and 8x table, stating and formal written Then demonstrate 20 divided by 5 is Show this as an array and talk using division facts for each methods 4 (how many jumps there are). about the distributive law eg multiplication fact show with the array that 12 x solve Explore multiplying TU numbers by 3 is the same as 10 x 3 add 2 x Explore multiplying TU problems, 2,5, and 10. Show this as an array and numbers by 2,5, 10, 3, 4 and including talk about the distributive law eg 8. Show this as an array and missing show with the array that 12 x 5 is the Use jottings to show stages of talk about the distributive number same as 10 x 5 add 2 x 5 calculation e.g. law eg show with the array problems, that 12 x 8 is the same as 10 (TU x U) involving ******* $32 \times 3 = (30 \times 3) + (2 \times 3)$ x 8 add 2 x 8. Show this with multiplication = 90 + 6 the array, grid method and in and division, 96 a formal method, but with including annotations positive Begin to talk about how the ****** integer scaling array can be shown as a grid, 10 problems and so that the items within the correspondenc Solve correspondence problems such array are not shown e problems in as how many different meals can you individually, with the array and which n order from a choice of 3 starters, grid shown side by side. objects are three main courses and three connected to desserts? Billy the clown wears a Divide numbers by 2,5,10, 3, ** m objects. nose and bowtie for his show. He has 4 and 8 using a sharing ** a red nose and a blue nose, and a strategy or a grouping spotted bowtie and a striped bow tie. strategy, recording with How many different outfits can he number sentences or appear in? How many outfits if he formally using $\sqrt{}$ for small buys a new nose and bow tie? numbers. 10 2 Divide numbers by 2,5,10 or 3 using a Solve problems, including sharing or a grouping strategy, missing number problems, recording with number sentences, measures and scaling, discuss dividing by 1 and by the deciding which operation to

	Divide numbers by 2,5,10, 3	use. Talk about remainders	
Explore associative law eg 2x 12 x 4 =	and 4 using a sharing strategy	in contexts	
8 x 12	or a grouping strategy,		
	recording with number		
	sentences, and link with		
	multiplication		
	Use place value to link facts eg		
	$4 \times 3 = 12, 40 \times 3 = 120, 4 \times 30$		
	$= 120, 120 \div 4 = 30 \text{ etc}$		

Year 4 Multiplication and Division

Term 1 and 2 Explore 6x and 9x table in terms of repeated addition, arrays and scaling, eg making a tower 6 times as tall or an amount 6 times as many Look for patterns in the multiples of 6 and 9, make links Term 3 and 4 Term 5 and 6 End of year recall multiplicati and rapid recall of all table facts to 12x 12 and related division for multiplicating tables and make Explore square numbers pictorially	on n facts cation
of repeated addition, arrays and scaling, eg making a tower 6 times as tall or an amount 6 times as many Look for patterns in the Explore 7, 11 and 12 table in terms of repeated addition, arrays and scaling. Look for patterns Explore 7, 11 and 12 table facts to 12x 12 and related division for multiplicating and division facts multiplicating and division facts facts to 12x 12 and related division for multiplicating and division facts 12	n facts cation
scaling, eg making a tower 6 times as tall or an amount 6 times as many Look for patterns in the Explore 7, 11 and 12 table in terms of repeated addition, arrays and scaling. Look for patterns Explore 7, 11 and 12 table facts to 12x 12 and related division for multiplicates tables up to 12	n facts cation
times as tall or an amount 6 in terms of repeated times as many Look for patterns in the in terms of repeated addition, arrays and scaling. Look for patterns in the scaling in terms of repeated addition, arrays and tables up to the scaling in terms of repeated addition, arrays and tables up to the scaling in terms of repeated addition, arrays and tables up to the scaling in terms of repeated addition, arrays and tables up to the scaling in terms of repeated addition.	cation
times as many addition, arrays and facts tables up to scaling. Look for patterns in the scaling. Look for patterns 12	
Look for patterns in the scaling. Look for patterns 12) 12 ×
multiples of 6 and 9, make links in the multiples and make Explore square numbers pictorially	
with 3x links between tables use place	
Practice recall of 6 and 9x table	
Make links between multiplying 12 table and use to solve multiplication eg and derived	t t
and dividing by 6 and 9, showing Make links between 16 x 7 = 4 x 4 x 7 facts to	
this practically or with an array multiplying and dividing multiply an or on a number line by 7, 11 and 12, showing Multiply two-digit and three-digit divide	a
this practically or with an numbers by a one-digit number mentally, array or on a number line using formal written layout, including:	
Multiply whole numbers by 0, 1, referring to the grid to show multiplying	by
10, 100, 1000, divide by 1, 10,, Multiply three numbers conceptual understanding 0 and 1;	Бу
100, 1000 etc together, using associative dividing by	1.
Use place value knowledge to law and commutative eg 4 multiplying	•
derive new facts eg $6 \times 9 = 54$ $\times 8 \times 5 = 20 \times 8$ Begin short division of TU by U together th	
so $60 \times 9 = 540, 540 \div 60 = 9$ etc which cannot be solved using table numbers	
Multiply HTU by U using facts alone, with numbers such as 3	
Solve problems involving the grid method and then $\sqrt{96}$ with no exchange and then recognise a	nd
multiplying and dividing, as formal long with exchange, using the fact that use factor p	oairs
including missing number multiplication one ten can be exchanged for ten and	
problems Eg 123 x 5 units and showing this with dienes commutative	vity
and / or place value counters eg 7 in mental	
$\sqrt{84}$ Model as sharing and calculations	5
Multiply TU by U, revising the grouping eg 84 shared between 7	
use of the array, grid and formal 123 people and how many groups of 7 multiply tw	_
method eg can you make from 84 (repeated and three-c	U
12 x5 subtraction) numbers by	
digit number	U
******* ** Sharing formal writ	ten
******* ** Some children may choose layout	
to use the expanded method of multiplication solve problems	oms
method of multiplication to understand before solve problem involving	E1115
to understand before involving multiplying	and
method e.g.	
using the	~~6
distributive	law to
multiply tw	o-digit



Year 5 Multiplication and Division

Term 1 and 2	Term 3 and 4	Term 5 and 6	End of year	l

Fluent and rapid recall of number facts to 12×12 and related division facts, and use these to derive other facts eg using place value $6 \times 7 = 42, 0.6 \times 7 = 4.2$

Use tables to identify all factor pairs of any number. Use and understand the term multiple.

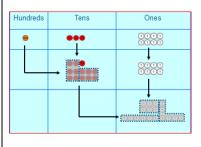
Consolidation of multiplying and dividing whole and decimal numbers by 10, 100 and 1000, especially when converting between metric units of measurement eg m and km, g and kg.

Recap the use of the array, grid method, expanded short multiplication and formal multiplication of HTU by U numbers as in Year 4. Use the distributive law eg calculate 123×6 with 100×6 , 20×6 and 3×6 and combining. Extend to ThHTU by U

Divide numbers up to HTU by one digit using the formal method of short division as set out in Year 4. Model exchange of one hundred with ten tens and one ten with ten units, with Dienes or place value counters.

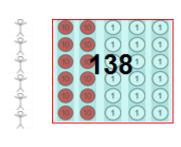
Explore as sharing and grouping (repeated subtraction)

138 divided by 6 as making groups of 6



6 \(\frac{23}{38} \)

138 divided by 6 as sharing between 6 people



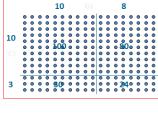
6 (38

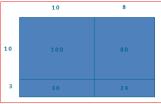
As before and

Find the common factors of pairs of numbers.

Define prime numbers as those with exactly two factors and find numbers which are prime and composite (not prime) up to 100

Multiply TU by TU using the array, grid and then expanded long multiplication and then formal long multiplication





18 <u>X13</u> 54 <u>180</u> 234

Use short division to divide ThHTU by one digit numbers as in terms 1 and 2, showing that one thousand can be exchanged for ten hundreds with dienes or place value counters for conceptual understanding

Use multiplication and division as inverses to solve problems and check solutions

As before and

Multiply and divide numbers mentally drawing on known facts

Recall prime numbers up to 19 Identify the prime factors of numbers, use and understand this language

Explore properties of square numbers

Multiply HTU by TU and ThHTU by TU using the grid and then expanded long multiplication and then formal multiplication

Consolidate use of short division for dividing numbers up to 4 digits by a one digit number. Interpret remainders in context eg talk about rounding an answer up or down based on the problem, decide and justify why they have shown as remainder as a remainder, a fraction or a decimal based on the problem they are solving.

Multiply and divide whole numbers and those involving decimals by 10, 100 and 1000

Recognise and use cube numbers, and the notation cubed (3)

Use the notation for squared and cubed numbers to write number sentences in different ways eg 3 x $270 = 3 \times 3 \times 9 \times 10 = 9^2 \times 10$

Solve problems involving addition, subtraction, multiplication and division and a identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers

know and use the vocabulary of prime numbers, prime factors and composite (nonprime) numbers

establish whether a number up to 100 is prime and recall prime numbers up to 19

multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers

multiply and divide numbers mentally drawing upon known facts

divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context

multiply and divide whole numbers and those involving decimals by 10, 100 and 1000

recognise and use square numbers and cube numbers, and the notation for squared (²) and

Recognise and use square numbers, and the notation for squared (²). Explore investigations with squared numbers such as how many squares on a chess board and the reindeer investigation (100 elves put 100 reindeers away for the night. Elf 1 turns the lock to the stables of reindeer 1,2,3,4 etc. Elf 2 turns the lock to the stables of reindeers 2,4,6,8... Elf 3 turns the lock to the stables of reindeers on. Which reindeer are locked up and which are not?)

combination of these, including understanding the meaning of the equals sign and deciding which operation to use

Solve problems involving multiplication and division, including scaling by simple fractions and problems involving simple rates, eg making something 3/7 as long, or find 4/5 of an amount. Explore 3 for 2 offers. Calculate rates such as the total for a family of 4 to go to a zoo knowing the price for adult and child tickets. Interpret scale drawings for example multiplying or dividing by 10, 100, 1000 etc

cubed (³)

solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign

solve problems involving multiplication and division, including scaling by simple fractions and problems involving simple rates.

Use the bar method to solve ratio problems

2. There are 32 children in a class.

There are 3 times as many boys as girls. How many girls?

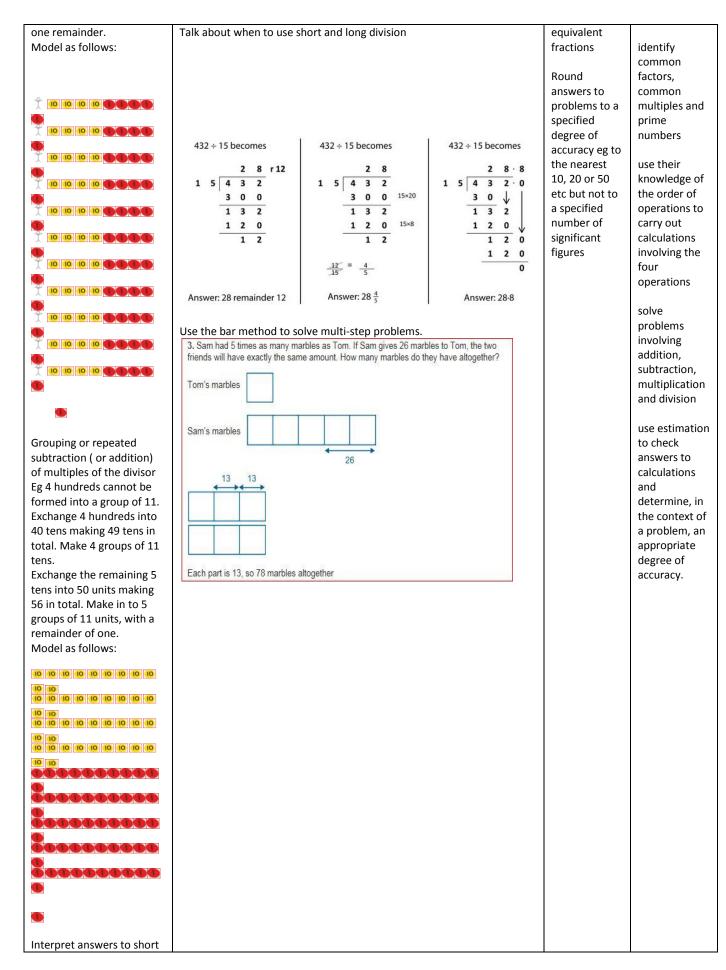
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32

Each square is 8, so there are 8 girls and 24 boys.

Year 6 Multiplication and Division

Term 1 and 2	Term 3 and 4	Term 5 and 6	End of year
Fluent and rapid recall of	As before and	As before and	multiply
number facts and use of			multi-digit
mental calculations	Recap long multiplication of numbers up to 4 digits by a two digit	Understand	numbers up
including solving problems	number, including with decimal numbers, using the grid method to	the use of	to 4 digits by
with more than one	secure conceptual understanding, and then moving to formal long	brackets.	a two-digit
operation and using large	multiplication, as set out in terms 1 and 2.	Explore the	whole
numbers		effect of	number using
		changing the	the formal
Recap long multiplication	Divide numbers up to 4 digits by a two-digit whole number using the	order of	written
of numbers up to 4 digits	formal written method of long division, as sharing and grouping	calculations	method of
by a one digit number,	For example:	eg 2 + (1 x 3)	long
including with decimal	121	= 5 and (2 + 1	multiplication
numbers, using the grid	15 1815) x 3 = 9	
method to secure		Use their	divide
conceptual understanding,		knowledge of	numbers up
and then moving to formal		the order of	to 4 digits by
long multiplication		operations to	a two-digit
Eg 2.37 x 3		carry out	whole
2 0.3 0.07	Sharing between 15 people:	calculations	number using the formal
	We can't share one thousand between 15 people, so exchange it for 10	involving the	
3 6 0.9 0.21	hundreds making 18 hundreds in total.	four	written
	Share one hundred to each of 15 people, subtract these from 1815.	operations	method of
2.37	Three hundred and 15 remain.	Solve	long division,
<u>X 3</u>	Exchange the three hundreds for 30 tens making 31 tens altogether.	problems	and interpret remainders
7.11	Share 2 tens to each of 15 people, subtract these from 315	involving	as whole
1 2	15 remain	addition,	number
	Exchange the one ten for ten units, making 15 in total	subtraction,	remainders,
Consolidate short division	Share one unit to each of 15 people, subtract these from 15.	multiplication	fractions, or
method, dividing numbers	None remain.	and division,	by rounding,
up to 4 digits by a two digit	Making groups of 15.	using	as
number, modelling this as	Making groups of 15:	estimation to	appropriate
sharing and grouping with	We can't form a group of 15 from one thousand, so exchange it for 10	check	for the
place value counters and	hundreds making 18 hundreds in total. Make one group of 15 hundreds, subtract this from 1815.	answers to	context
dienes, exchanging one	Three hundred and 15 remain.	calculations	
thousand for ten hundreds,	Exchange the three hundreds for 30 tens making 31 tens altogether.	and	divide
one hundred for ten tens	Make 2 groups of 15 tens, subtract these from 315.	determine, in	numbers up
and one ten for ten units.	15 remain	the context	to 4 digits by
Eg	Exchange the one ten for ten units, making 15 in total	of a problem,	a two-digit
	Share one unit to each of 15 people, subtract these from 15.	an	number using
4 5 r1	None remain.	appropriate	the formal
5	Notice remains	degree of	written
1 1 4 9 6		accuracy.	method of
	Interpret answers to long division in the context of the problem, eg as		short division
	whole number remainders, or as fractions or by rounding up or down,	Identify and	where
Sharing	justifying their decision according to the problem they are solving.	explore	appropriate,
Sharing Eg sharing 496 between 11	, , , , , , , , , , , , , , , , , , ,	common	interpreting
people. 4 hundreds cannot		factors,	remainders
be shared between 11		common	according to
people so exchange 4		multiples and	the context
hundreds for 40 tens,		prime	_
making 49 tens in total.		numbers eg	perform
Each person has 4 tens.		which	mental
Exchange the remaining 5		numbers have	calculations,
tens into 50 units making		odd totals of	including
56 in total. Share these		factors? Link	with mixed
between the 11 people,		common	operations
giving 5 to each, leaving		factors to	and large
grange to eath, leaving		finding	numbers



Palace Wood Primary Progression in Calculation document

division in the context of		
the problem, eg as whole		
number remainders, or as		
fractions or by rounding up		
or down, justifying their		
decision according to the		
problem they are solving.		